

CS-Statistics	Central Limit Theorem and Confidence Intervals
Tutorial 6	

1. An unknown distribution has a mean of 90 and a standard deviation of 15. Samples of size $n = 25$ are drawn randomly from the population.
 - a) Find the probability that the sample mean is between 85 and 92.
 - b) Find the value that is two standard deviations above the expected value of the sample mean.
2. An unknown distribution has a mean of 90 and a standard deviation of 15. A sample of size 80 is drawn randomly from the population.
 - a) Find the probability that the sum of the 80 values (or the total of the 80 values is more than 7500.
 - b) Find the sum that is 1.5 standard deviations above the mean of the sums.
3. In a recent study, the mean age of tablet users is 35 years. Suppose the standard deviation is ten years. The sample size is 39.
 - a) What are the mean and standard deviation for the sum of the ages of tablet users? What is the distribution?
 - b) Find the probability that the sum of the ages is between 1,400 and 1,500 years.
 - c) Find the 90th percentile for the sum of the 39 ages.
4. Interval estimation in large samples. Unknown distribution. Suppose that an accounting firm does a study to determine the time needed to complete one person's tax forms. It randomly surveys 100 people. The sample mean is 23.6 hours. There is a known standard deviation of 7.0 hours.
 - a) Construct a 90% confidence interval for the population mean time to complete the tax forms.
 - b) If the firm wished to increase its level of confidence and keep the error bound the same by taking another survey, what changes should it make?
 - c) If the firm did another survey, kept the error bound the same, and only surveyed 49 people, what would happen to the level of confidence? Why?
 - d) Suppose that the firm decided that it needed to be at least 99% confident of the population mean length of time to within one hour. How would the number of people the firm surveys change? Why?
5. A random sample of statistics students were asked to estimate the total number of hours they spend looking at their mobiles during an average day. The responses are: 0, 3, 1, 20, 9, 5, 10, 1, 10, 4, 5, 14, 4, 5, 2. Use this sample data to construct a 98% confidence interval for the mean number of hours statistics students will spend on the mobiles.