

CS-Statistics	<b>More on Normal Distribution</b>
Tutorial 5	

1. Heights of 25 -year-old men in a certain region have mean 69.75 inches and standard deviation 2.59 inches. These heights are approximately normally distributed. Sketch a qualitatively accurate graph of the density function for  $X$  .
  - a) Find the probability that a randomly selected 25 -year-old man is more than 69.75 inches tall.
  - b) Find the probability that a randomly selected 25 -year-old man is more than 72 inches tall.
  
2. The RV  $Z$  has a standard normal distribution.
  - a) Find the value  $z^*$  of  $Z$  so that  $P(Z < z^*) = 0.0125$ . The value  $z^*$  is a cuts off a left tail of area 0.0125 in the standard normal distribution,
  - b) Find the value  $z^*$  of  $Z$  so that  $P(Z > z^*) = 0.0250$ . The value  $z^*$  is a cuts off a right tail of area 0.0250 in the standard normal distribution,
  - c) Find the values  $za$  such that:  $P(-za < Z < za) = 0.68$  and  $P(-za < Z < za) = 0.95$   
You need the statistical tables, see, for example, [here](#).
  
3. The lifetimes of the tread of a certain automobile tire are normally distributed with mean 37,500 km and standard deviation 4,500 km. Find the probability that the tread life of a randomly selected tire will be between 30,000 and 40,000 km.
  
4. The final exam scores in a statistics class were normally distributed with a mean of 63 and a standard deviation of five.
  - a) Find the probability that a randomly selected student scored more than 65 on the exam.
  - b) Find the probability that a randomly selected student scored less than 80
  - c) Find the 90th percentile (that is, find the score  $k$  that has 90% of the scores below  $k$  and 10% of the scores above  $k$ ).
  - d) Find the 70th percentile (that is, find the score  $k$  such that 70% of scores are below  $k$  and 30% of the scores are above  $k$ ).